

Chemical effects on ecological interactions within a model-experiment loop

September 13, 2022

Dominique Lamonica^{1,2*} Sandrine Charles¹ Bernard Clément² & Christelle Lopes¹

¹ Université de Lyon, F-69000, Lyon; Université Lyon 1; CNRS, UMR 5558, Laboratoire de Biométrie et Biologie Evolutive, F-69622, Villeurbanne, France

² Université de Lyon, F-69000, Lyon; Université Lyon 1; ENTPE; CNRS, UMR 5023, Laboratoire d'Ecologie des Hydrosystèmes Naturels et Anthropisés; 3, rue Maurice Audin, 69518 Vaulx-en-Velin, France

* dominique.lamonica@univ-lyon1.fr

Keywords: Bayesian inference ; microcosm ; experimental design optimisation ; cadmium ; daphnid ; duckweed ; microalgae

Abstract

We propose in this paper a method to assess the effects of a contaminant on a micro-ecosystem, integrating the population dynamics and the

4 interactions between species. For that, we developed a dynamic model to
5 describe the functioning of a microcosm exposed to a contaminant and
6 to discriminate direct and indirect effects. Then, we get back from mod-
7 elling to experimentation in order to identify which of the collected data
8 have really been necessary and sufficient to estimate model parameters in
9 order to propose a more efficient experimental design for further investi-
10 gations. We illustrated our approach using a 2-L laboratory microcosm
11 involving three species (the duckweed *Lemna minor*, the microalgae *Pseu-*
12 *dokirchneriella subcapitata* and the daphnids *Daphnia magna*) exposed to
13 cadmium contamination. We modelled the dynamics of the three species
14 and their interactions using a mechanistic model based on coupled ordi-
15 nary differential equations. The main processes occurring in this three-
16 species microcosm were thus formalized, including growth and settling of
17 algae, growth of duckweeds, interspecific competition between algae and
18 duckweeds, growth, survival and grazing of daphnids, as well as cadmium
19 effects. We estimated model parameters by Bayesian inference, using si-
20 multaneously all the data issued from multiple laboratory experiments
21 specifically conducted for this study. Cadmium concentrations ranged be-
22 tween 0 and 50 $\mu\text{g.L}^{-1}$. For all parameters of our model, we obtained
23 biologically realistic values and reasonable uncertainties. The cascade of
24 cadmium effects, both direct and indirect, was identified. Critical effect
25 concentrations were provided for the life history traits of each species. An
26 example of experimental design adapted to this kind a microcosm was also
27 proposed. This approach appears promising when studying contaminant
28 effects on ecosystem functioning.

29 **1 Introduction**

30 The toxic effects of contaminants are most often studied at the individual level,
31 since it is easier to study life history traits of an isolated organism, studying for
32 example its survival, development or capacity to reproduce. Moreover, monospe-
33 cific bioassays are easy to implement and perform, and observation data at the
34 individual level are straightforward to analyse, since they depict the direct ef-
35 fects of contaminants. Nevertheless effects can also be measured at other levels
36 of biological organisation using various experimental devices that are chosen
37 related to the level of interest, by adapting several characteristics such as size,
38 duration, number of species, abiotic compartment, etc [Calow, 1993]. Multi-
39 species devices, like microcosms and mesocosms, allow to study organisation
40 levels from populations to ecosystem, by integrating population dynamics and
41 interactions between species [Forbes et al., 1997, Kimball and Levin, 1985, Ra-
42 made, 2002]. However, extrapolating toxic effects from one biological level to
43 the next based on observation data remains a challenge. In particular, going
44 from individual to population levels, or from population to community levels,
45 implies taking into account intra- and inter-specific interactions, which are of
46 major importance in the functioning of ecosystems, while it is necessary to in-
47 tegrate these interactions for a better assessment of the ecotoxicological risk
48 [Cairns, 1984, De Laender et al., 2008, Preston, 2002].

49 Modelling tools have proven their utility to analyse ecotoxicological data, by
50 highlighting the underlying mechanisms leading to observations at each level
51 of biological organisation. But modelling appears particularly helpful when ex-
52 trapolation of contaminant effects from biological levels reveals necessary. For
53 instance, physiologically based toxico-kinetic survival models allow to extrapo-

54 late the fate of a contaminant at sub-individual level to its effects on individual
55 survival [Ashauer et al., 2016], or individual based models (IBM) including con-
56 taminant permit to extrapolate effects on the population level from effects on
57 the individuals [Hansul et al., 2021, Mintram et al., 2018], or food web models
58 permit to transfer effects of contaminants across the whole community [Baudrot
59 et al., 2018].

60 Ecotoxicology relies on experimental data, while being concerned by the Re-
61 placement, Refinement and Reduction of Animals in Research (3Rs) program
62 [Kilkenny et al., 2009] and by difficulties linked to collection of field data. Taking
63 the most of experimental data and reducing the amount of experiments to per-
64 form in general is a key issue the ecotoxicology field faces. Formal optimisation
65 of experimental design can be applied to standard tests (namely monospecific
66 bioassays): they have been questioned in terms of test duration and measured
67 endpoints [Charles et al., 2016] or regarding the tested concentration range
68 [Forfait-Dubuc et al., 2012]. Yet, more complex experimental designs, like mi-
69 crocosms or mesocosms may resist to formal optimisation particularly because
70 of species interactions leading to indirect effects. Some attempts have been
71 made in simple cases to deal with standard dose-responses curves [Chèvre and
72 Brazzale, 2008, Holland-Letz and Kopp-Schneider, 2015, Keddig et al., 2015,
73 Khinkis et al., 2003, Sitter and Torsney, 1995, Wang et al., 2006] but to our
74 knowledge, nothing similar exist for multi-species models. Nevertheless, when
75 modelling has been integrated to the experimental framework, it can easily be
76 used to evaluate *a posteriori* the relevance of the data, as a pragmatic and
77 case-by-case method to analyse the information provided by data and possibly
78 improve the experimental design for studies with microcosm experiments with

79 similar species and compounds.

80 The aim of our paper is to illustrate (1) how to use modelling to describe the
81 functioning of a three-species microcosm exposed to a contaminant and to dis-
82 criminate direct effects (related to effects on specific, modelled processes) and
83 indirect effects (related to effects resulting from the cascade of processes); (2)
84 how to develop critical effect concentrations for key population regulating pro-
85 cesses (such as EC_{50} in stress functions); and (3) how model outcomes can
86 inform experimental design in order to identify which of the collected data have
87 really been necessary and sufficient to estimate model parameters in order to
88 propose a more efficient experimental design for further investigations.

89 Different steps have been set up to achieve our objectives, as summarised in
90 Figure 1. We performed experiments to collect data on the microcosm species
91 populations at different cadmium concentrations. In parallel, we formulated a
92 model of the microcosm functioning under a chemical stressor based on cou-
93 pled ordinary differential equations (ODE) and effect functions. First, using all
94 data we estimated model parameters, in particular those related to effect func-
95 tions (Figure 1, black boxes). Using data where species occur in isolation and
96 where they occur as a community of species permitted to identify direct and
97 indirect effects of cadmium on the population dynamics of the different species.

98 We then globally analysed the perturbations of our small community (objective
99 1). We also extracted EC_{50} for the different processes (growth, survival, and
100 strength of interspecies interaction) (Figure 1, orange boxes). In order to assess
101 the relevance of certain data, we removed those data from the complete dataset
102 to build partial datasets. Then, we estimated function parameters with the
103 partial datasets. The newly estimated effect functions were then compared to

104 the reference ones obtained with the complete dataset (Figure 1, green boxes).
105 This allowed us to evaluate the added values of only considering partial datasets
106 instead of the complete original one (objective 2).

107 2 Experiments and observed data

108 **Experimental design** Microcosms were identically prepared for all experi-
109 ments according to [Lamonica et al., 2016a] ([without sediment](#)). Algae, duck-
110 weeds and daphnids were cultivated at the laboratory according to internal
111 protocols [Clément et al., 2014]. According to the experiment, beakers were
112 inoculated with one, two or three species at the start of the experiment (day
113 0). When algae were present, 4.10^7 cells of *P. subcapitata* were introduced into
114 beakers. When daphnids were present, 10 daphnids (*Daphnia magna* neonates
115 aged 24 ± 12 h) were introduced into beakers. When duckweeds were present, 8
116 fronds of duckweeds were introduced into beakers. The algal density in the water
117 column was measured every two to three days with a particle counter [Lamon-
118 ica et al., 2016a]. The algal density at the bottom of the beakers was measured
119 once during the experiment [Lamonica et al., 2016b]. Daphnids neonates were
120 removed from the microcosm every two days, meaning that reproduction was
121 considered as an independent process in the microcosm functioning [Lamon-
122 ica et al., 2016a]. The number of daphnids in each beaker was counted (after
123 neonate removal if necessary) and their size measured (from the centre of the
124 eye to the caudal base of spine) twice or thrice per week. The duckweed fronds
125 were counted every two to three days. The experiments lasted between 13 and
126 21 days. [The experiments are summarised in SI Table S1.](#)

127 **Experiments without cadmium** Experiment 1 involved algae and daphnids
128 as detailed in [Lamonica et al., 2016a] (referred [in that paper](#) as "Experiment
129 without sediment" in section 2.3.2.). Experiment 2 involved algae alone as
130 detailed in [Lamonica et al., 2016b] (referred [in that paper](#) as "Experiment 1"
131 in section 2.2.1.). Experiment 3 involved algae and duckweeds as detailed in
132 [Lamonica et al., 2016b] (referred [in that paper](#) as "Experiment 3" in section
133 2.2.2.).

134 **Experiments with cadmium** Experiment 4 involved algae and duckweeds,
135 with two conditions in species composition: duckweeds alone, and algae and
136 duckweeds together. We tested five different cadmium concentrations (0, 11.1,
137 20.2, 35.5 and 51.1 $\mu\text{g/L}$) in triplicate for each condition. Three additional con-
138 trol beakers were inoculated with algae alone. The duration of this experiment
139 was 14 days. From this experiment, we obtained different types of data un-
140 der contaminant exposure: "monospecific data, duckweeds", "two species data,
141 duckweeds" and "two species data, algae".

142 Experiment 5 involved the three species, with three conditions in species com-
143 position: duckweeds alone, algae and duckweeds, and algae, duckweeds and
144 daphnids. We tested five different cadmium concentrations in triplicate for each
145 condition (0, 2.25, 4.50, 6.88 and 9.09 $\mu\text{g/L}$). The duration of this experiment
146 was 21 days. From this experiment, we obtained the following data under con-
147 taminant exposure: "monospecific data, duckweeds"; "two species data, duck-
148 weeds" and "two species data, algae"; "complete microcosm data, duckweeds",
149 "complete microcosm data, algae" and "complete microcosm data, daphnids".

150 Experiment 6 involved algae alone. We tested five different cadmium concen-

151 trations (0, 26.2, 36.4, 40.8 and 43.6 $\mu\text{g/L}$) in triplicate. The duration of this
152 experiment was 14 days. From this experiment, we obtained "monospecific data,
153 algae".

154 As mentioned in [Lamonica et al., 2016b], we used measured cadmium concen-
155 trations in the medium instead of nominal ones. For that purpose, we measured
156 dissolved cadmium concentrations as described by Clement et al. [Clément et al.,
157 2014] at days 2, 7, 14 (and day 21 for Experiment 5) in each beaker. We then
158 calculated the arithmetic mean of all the measurements. In total, for Experi-
159 ments 4, 5 and 6, we thus obtained 13 concentrations (0, 2.25, 4.50, 6.88, 9.09,
160 11.1, 20.2, 35.5, 51.1, 26.2, 36.4, 40.8 and 43.6 $\mu\text{g/L}$) denoted by C_j , $j \in [0, 12]$
161 hereafter. The concentration in the controls of Experiments 4, 5 and 6 (that is
162 with no contaminant) is denoted by C_0 , corresponding to index $j = 0$. This is
163 also the case in Experiments 1 to 3, that were conducted without contaminant.

164 **3 Dynamic modelling**

165 The description of the model follows the Overview, Design concepts and De-
166 tails (ODD) protocol originally used for describing individual and agent-based
167 models Grimm et al. [2010] but adapted here for a dynamic model based on
168 Ordinary Differential Equations (ODE). The ODD protocol consists of seven
169 elements. The first three elements provide an overview; the fourth element ex-
170 plains general concepts underlying the model's design and the remaining three
171 elements provide further details.

172 **3.1 Purpose**

173 The model developed in this paper describes the dynamics of duckweeds, al-
174 gae and daphnids under the microcosm conditions described in "Experiments
175 and observed data" section. In particular, it aims at i) comparing the species
176 dynamics both in isolation and together in order to highlight the interactions
177 between the three species; and ii) describing the effects of cadmium on the dif-
178 ferent processes involved in the microcosm functioning. We first present the
179 model of the three species' dynamics without contaminant, then we show how
180 we integrated cadmium effects in the model.

181 **3.2 Entities, state variables and scales**

182 We model both duckweed and algal population dynamics but we only model
183 two daphnid life history traits (growth and survival) that are involved in the
184 interaction between algae and daphnids. The model involves five state variables.
185 The two first ones refer to the numbers of algal cells per beaker in the two
186 compartments of the microcosm at time t and cadmium concentration C_j : the
187 suspended algae in the water column (Compartment 1), denoted by $N_1(t, C_j)$,
188 and the settled algae at the bottom of the beaker (Compartment 2), denoted
189 by $N_2(t, C_j)$. The third state variable is the number of duckweed fronds per
190 beaker at time t and cadmium concentration C_j , denoted by $N_d(t, C_j)$. The
191 two other state variables refer to the daphnids: the number of alive daphnids in
192 the microcosm through survival rate at time t and cadmium concentration C_j ,
193 denoted by $S(t, C_j)$ and the daphnid size at time t and cadmium concentration
194 C_j , denoted by $L(t, C_j)$. The model is run on 21 days, corresponding to the
195 duration of the longest experiment.

196 **3.3 Process overview and scheduling**

197 Nine processes are modelled with a continuous time scale, using ODE. Two
198 processes are related to intrinsic algal dynamics: settling of suspended algae
199 and growth of both suspended and settled algae. One process is related to
200 intrinsic duckweed dynamics: duckweed growth. One process concerns the
201 algae-duckweed interaction with an interspecific competition. Two processes
202 are related to daphnid life history traits: survival and growth. Two processes
203 are related to algae-daphnid interaction: ingestion of algae by daphnids and
204 location of daphnid for grazing. The last process is related to the effects of
205 cadmium on the different parameters. An overall graphical representation of
206 the implemented model is given in Figure S1.

207 **3.4 Design concepts**

208 **3.4.1 Basic principles**

209 The assumptions we make are based on the experimental design described in
210 "Experiments and observed data" section. We assume that algae are uniformly
211 distributed in the water column and at the bottom of the beaker at each time
212 step and that the settling speed of suspended algae is constant throughout
213 the water column. Therefore, the water volume occupied by the suspended
214 algae is supposed to decrease at the same speed as algal settling. We assume
215 that algae and duckweeds are competing only for nutrients in the medium.
216 We also assume that settled algae are too distant from duckweeds to interact
217 with them, so that the interspecific competition only involves suspended algae.
218 Interspecific competition has no effect on algae, as shown in Lamonica et al.

219 [2016b]. We assume that cadmium affects the growth rates of all species, as
220 well as competition intensity parameters and daphnid survival. Cadmium is
221 supposed not to affect either the carrying capacities of algae and duckweeds or
222 the algal settling rate.

223 **3.4.2 Emergence**

224 Algal and duckweed dynamics emerge both from their intrinsic dynamics (growth
225 and settling for algae, growth for duckweeds) and from the interspecific com-
226 petition between the two species. Algal dynamics also depends on daphnids
227 through the quantity of algal cells that are consumed by daphnids. With cad-
228 mium, both dynamics emerge from the impact of cadmium on their respective
229 growth and on the interaction.

230 **3.4.3 Sensing**

231 In order to determine the number of daphnids grazing in each compartment
232 over time, we assume that daphnids, as pelagic species, preferentially feed in
233 the water column Siehoff et al. [2009]. We also assume that daphnids move
234 to the sediment when the ratio of algal density in the water column over the
235 bottom of the beaker is below a given threshold Siehoff et al. [2009].

236 **3.4.4 Interactions**

237 Intraspecific competition between algal cells and between duckweed colonies
238 are taken into account in their respective logistic growth models. Algae and
239 duckweeds interact through an interspecific competition process, described with
240 a Lotka-Volterra type I interaction model. Algae and daphnids interact through
241 a trophic relationship, namely grazing.

242 **3.4.5 Stochasticity**

243 We use stochasticity to describe variability on state variables, which sum up
244 both uncertainties and variability sources within the processes. We suppose
245 a normal distribution on the decimal logarithm of the number of algal cells
246 per beaker in each compartment (in the water column and at the bottom of
247 the beaker) Roger and Reynaud [1978] and on the decimal logarithm of the
248 number of duckweed fronds. For the number of daphnid survivors we consider
249 a conditional binomial distribution Forfait-Dubuc et al. [2012] and a normal
250 distribution for the daphnid size.

251 **3.5 Initialisation**

252 As algae are inoculated in the water column only, the initial values for the
253 number of algal cells per beaker in the water column and at the bottom of the
254 beaker are 4×10^7 and 0, respectively. The initial number of duckweed fronds is
255 8. The initial number of daphnids is 10, the initial survival rate is fixed to 1 (as
256 all introduced daphnids are alive) and the initial daphnid size is drawn from a
257 normal distribution (see hereafter section 4.1). As mentioned in section 2., we
258 use measured cadmium concentrations 0, 2.25, 4.50, 6.88, 9.09, 11.1, 20.2, 35.5,
259 51.1, 26.2, 36.4, 40.8 and 43.6 $\mu\text{g/L}$.

260 **3.6 Input data**

261 The model does not use input data to represent time-varying environmental
262 processes. Laboratory conditions are controlled and supposed to be constant
263 over time.

264 **3.7 Submodels**

265 All information on parameters and variables involved in the model are gathered
266 together in SI Table S2. Details about parameter estimation are given in "Sta-
267 tistical inference" section.

268 The deterministic part of algal dynamics in both compartments and of duck-
269 weed dynamics over time t (in days) is described with three coupled ODE. The
270 deterministic part of daphnid survival and size are described with two other
271 ODE that are presented in their integrated form.

272 **3.7.1 Algae processes**

273 We model the algae dynamics using logistic functions to describe algae growth
274 in the water column and at the bottom of the beaker. We used an exponential
275 decay of algal cells in the water column to describe sedimentation process.

276 **3.7.2 Duckweed process**

277 We model the duckweed growth using a logistic function.

278 **3.7.3 Daphnid processes**

279 **Survival** Survival rate at time t and cadmium concentration C_j , $S(t, C_j)$, is
280 described by an exponential decay with an instantaneous mortality rate, m_0
281 (day^{-1}), which is assumed to be time-independent Forfait-Dubuc et al. [2012]:

$$S(t, C_j) = \exp(-(m_0 + k_s \times \max(0, C_j - NEC)) \times t) \quad (1)$$

282 where k_s ($\mu\text{g}^{-1} \cdot \text{L} \cdot \text{day}^{-1}$) represents the cadmium effect intensity and NEC
283 (No Effect Concentration) ($\mu\text{g} \cdot \text{L}^{-1}$) is the concentration from which the con-

284 contaminant has an effect on survival. When concentration C_j is below the NEC ,
 285 $\max(0, C_j - NEC)$ is equal to 0, thus there is no effect on survival rate which
 286 only depends on natural mortality m_0 and time t . However, when concentra-
 287 tion C_j is superior to the NEC , $\max(0, C_j - NEC)$ is equal to the surplus of
 288 concentration and mortality due to cadmium is added to the natural mortality.
 289 We consider a conditional binomial stochastic model for $D_s(t, C_j)$, the num-
 290 ber of alive daphnids at time t and cadmium concentration C_j in the system
 291 Forfait-Dubuc et al. [2012]:

$$D_s(t, C_j) \sim \mathcal{B} \left(\frac{S(t, C_j)}{S(t-1, C_j)}, D_s(t-1, C_j) \right) \quad (2)$$

292 where \mathcal{B} stands for the binomial law. For each concentration C_j , the number
 293 of alive daphnids at time t depends on the number of alive daphnids at time
 294 $t-1$ and on the survival probability between $t-1$ and t , represented by $\frac{S(t)}{S(t-1)}$.
 295 We make here the implicit assumption that contaminant toxicokinetics is fast
 296 (which means that internal concentration in the organism is supposed to be equal
 297 to external concentration in the water C_j) since cadmium have been shown to
 298 have a rapid toxicokinetic, especially a high capacity of bioaccumulation, at
 299 least in freshwater organisms [Gestin et al., 2021, Ratier and Charles, 2022].

300 **Growth** Daphnid growth is described using a Von Bertalanffy growth model
 301 Von Bertalanffy [1938]. In addition, the daphnid size is supposed to follow a
 302 normal distribution with mean $L(t, C_j)$ and standard deviation σ_L .

303 3.7.4 Interaction processes

304 **Interspecific competition process** We model the interspecific competition
 305 process between algae and duckweed using a unilateral Lotka-Volterra type I

306 model, with an effect on duckweed dynamics only.

307 **Ingestion process** The ingestion rate of a daphnid, *i.e.* the number of cells
 308 per beaker each daphnid consumes per day (denoted as $g_1(t, C_j)$ in the water
 309 column and $g_2(t, C_j)$ at the bottom of the beaker) is modelled with a Holling
 310 type II function of algal density in each compartment ($\frac{N_1(t, C_j)}{V_1(0)}$ and $\frac{N_2(t, C_j)}{V_2}$),
 311 for a given daphnid size $L(t, C_j)$:

$$g_1(t, C_j) = \frac{\delta_2 \times L(t, C_j)^\gamma \times \frac{N_1(t, C_j)}{V_1(0)}}{\delta_3 + \frac{N_1(t, C_j)}{V_1(0)}} \quad (3)$$

312 and

$$g_2(t, C_j) = \frac{\delta_2 \times L(t, C_j)^\gamma \times \frac{N_2(t, C_j)}{V_2}}{\delta_3 + \frac{N_2(t, C_j)}{V_2}} \quad (4)$$

313 with δ_2 (cell.daphnd⁻¹.day⁻¹.mm^{-γ}) the maximum ingestion rate, δ_3 (cell.mL⁻¹)
 314 the algal density for which the ingestion rate is equal to half the maximum
 315 ingestion rate and γ (dimensionless) a regression coefficient.

316 **Grazing location** The number of daphnids grazing in the water column at
 317 time t and cadmium concentration C_j , $D_1(t, C_j)$, is modelled with respect to
 318 the ratio $R(t, C_j)$ of algal density in compartment 1 over compartment 2 and
 319 the number of alive daphnids per beaker $D_s(t, C_j)$:

$$D_1(t, C_j) = \frac{D_1(t, C_j)R(t, C_j)}{\delta R(t, C_j)} \quad (5)$$

320 3.7.5 Cadmium effects

321 We suppose that the survival process is affected by cadmium according to Eq.(5).

322 We suppose that only growth rates and parameters of competition intensity

323 are affected by cadmium, as already assumed in Lamonica et al. [2016b]. We
 324 choose a three-parameter log-logistic function to describe the effect of cadmium
 325 at concentration C_j on each affected parameter p :

$$p(C_j) = \frac{p_0}{1 + \left(\frac{C_j}{E_p}\right)^{b_p}} \quad (6)$$

326 where p_0 is the value of parameter p in the control, E_p is the cadmium
 327 concentration at which $p(C_j) = \frac{p_0}{2}$, which is equivalent to an EC_{50} , and b_p is
 328 the curvature coefficient of the log-logistic function.

329 3.7.6 Complete model

330 Finally, the deterministic part of the model describing the functioning of the
 331 whole microcosm is expressed as follows:

$$\left\{ \begin{array}{l} \frac{dN_1(t, C_j)}{dt} = \frac{r_{a_0}}{1 + \left(\frac{C_j}{E_{r_a}}\right)^{b_{r_a}}} \times N_1(t, C_j) \times \left(1 - \frac{N_1(t, C_j)}{K_1(0) \exp(-s \times t)}\right) - s \times N_1(t, C_j) \\ - \frac{D_s(t, C_j) R(t, C_j)}{\delta + R(t, C_j)} \times g_1(t, C_j) \\ \frac{dN_2(t, C_j)}{dt} = \frac{r_{a_0}}{1 + \left(\frac{C_j}{E_{r_a}}\right)^{b_{r_a}}} \times N_2(t, C_j) \times \left(1 - \frac{N_2(t, C_j)}{K_2}\right) + s \times N_1(t, C_j) \\ - (D_s(t, C_j) - \frac{D_s(t, C_j) R(t, C_j)}{\delta + R(t, C_j)}) \times g_2(t, C_j) \\ \frac{dN_d(t, C_j)}{dt} = \frac{r_{d_0}}{1 + \left(\frac{C_j}{E_{r_d}}\right)^{b_{r_d}}} \times N_d(t, C_j) \times \left(1 - \frac{N_d(t, C_j)}{K_d}\right) - \frac{\beta_0}{1 + \left(\frac{C_j}{E_{\beta}}\right)^{b_{\beta}}} \times N_d(t, C_j) \times N_1(t, C_j) \\ L(t, C_j) = L_{\infty} - (L_{\infty} - L_0) \times \exp\left(-\frac{k_0}{1 + \left(\frac{C_j}{E_k}\right)^{b_k}} \times t\right) \\ S(t, C_j) = \exp(-(m_0 + k_s \times \max(0, C_j - NEC)) \times t) \end{array} \right. \quad (7)$$

332 The same model can be applied when daphnids are absent, by setting $D_s(t, C_j) =$
 333 0 and thus $D_1(t, C_j) = 0$. In this case, the two last equations must also be re-
 334 moved. The same model can be applied when duckweeds are absent, by setting
 335 $N_d(t, C_j) = 0$ and removing the third equation. The same model can be applied

336 when algae are absent, by setting $N_1(t, C_j) = 0$ and removing the first two
337 equations. When the water column is stirred (*i.e.* when algae are supposed not
338 to settle and duckweeds and daphnids are absent), the settling rate s is assumed
339 to be zero and the second and two last equations must be removed.

340 At each time step, the decimal logarithm of the number of algal cells per beaker
341 in the water column follows a normal distribution of mean $N_1(t, C_j)$ and stan-
342 dard deviation σ_{N_1} . The decimal logarithm of the number of algal cells per
343 beaker on the sediment follows a normal distribution of mean $N_2(t, C_j)$ and
344 standard deviation σ_{N_2} . The decimal logarithm of the number of duckweed
345 fronds per beaker follows a normal distribution of mean $N_d(t, C_j)$ and standard
346 deviation σ_{N_d} .

347 **4 Statistical inference**

348 In order to check if our model satisfactorily described the microcosm functioning,
349 we used Bayesian inference to fit the model simultaneously to all our experi-
350 mental data from the six above mentioned experiments. Estimates obtained for
351 all the parameters are called "reference estimates" hereafter.

352 **4.1 Parameter prior distributions**

353 We defined prior distributions summarising all information on each parameter
354 available in advance (SI Table S2). Some of the prior distributions described
355 the decimal logarithm of the parameter because of an expected large range of
356 possible values (for instance, b_{r_d} , k_S , and β_0) or extreme orders of magnitude
357 (*e.g.*, large or small). Other prior distributions were defined based on previous
358 experiments that were conducted using the same experimental device [Billoir

359 et al., 2011, 2012, Delhaye, 2011, Lamonica et al., 2016a] (r_{a_0}), or based on
360 additional experiments specifically conducted in the laboratory (E_{r_a} , b_{r_a} , r_{d_0} ,
361 β_0). At last, the remaining distributions were based on literature values [Billoir
362 et al., 2008, Biron et al., 2012, DeMott, 1982, Egloff and Palmer, 1971] (k_0),
363 except for parameters on which we had very vague information (E_β , b_β , b_{r_d}), so
364 that their prior distributions were chosen as flat.

365 4.2 Computation

366 Monte Carlo Markov Chain (MCMC) computations were performed using the
367 JAGS software via the *rjags* R package [Plummer, 2009, Team, 2013], after the
368 model was discretised using the Euler method with a time step equal to 0.1 as
369 stated in [Lamonica et al., 2016a]. Three chains were run. A total of 20000
370 iterations was performed as a burn-in phase and inference was based on 100000
371 additional iterations for each of the three chains. To check the convergence of
372 the estimation process, we used the Gelman and Rubin convergence diagnostic
373 [Gelman and Rubin, 1992] [with a cut-off of 1.01](#).

374 4.3 Posterior Predictive Check

375 To check posterior predictions of the model, we simulated new data at all ex-
376 perimented time steps and tested concentrations taking into account parameter
377 uncertainties and stochasticity of the model [Lamonica et al., 2016a]. 95% of
378 the observed data are expected to be contained in the 95% credibility band of
379 the predicted data, got from 2.5% and 97.5% percentiles of the predictions.

380 **5 Look-back on the experimental design**

381 We aim at determining which types of data could be sufficient to accurately (in
382 terms of mode of the posterior distribution) and precisely (in terms of dispersion
383 of the posterior distribution) estimate parameters of stress functions for the dif-
384 ferent species (Table 1). Our reference was the posterior distributions obtained
385 when estimating parameters from the whole dataset, considering them as the
386 "best possible estimates in the present case study in view of the model and
387 all available data". To evaluate the information provided by certain data, we
388 built partial datasets by removing these data from the whole dataset. Then, we
389 re-estimated the model parameters using these partial datasets and compared
390 the newly obtained estimates with the reference ones.

391 Four partial datasets (numbered A to D) were used to estimate the stress func-
392 tion parameters. They are summarized in Table 2. We evaluated only informa-
393 tion provided by data collected under contaminated conditions, removing them
394 successively to build the partial datasets. Regarding data without contami-
395 nant, including the controls in Experiments 4 to 6, they were kept in all partial
396 datasets.

397 Dataset A included all data except the "monospecific data" with contaminant.
398 This corresponds to exclude data collected from beakers containing only one
399 species. Thus, data from Experiment 6 and data "duckweeds alone" from Ex-
400 periments 4 and 5 were not included in dataset A. Dataset B included all data
401 except the "two species data" with contaminant. This corresponds to exclude
402 data collected from beakers with both duckweeds and algae. Thus, duckweed
403 and algae data collected from beakers containing both duckweeds and algae
404 from Experiments 4 and 5 were not included in dataset B. In dataset C, we

405 only included the "complete microcosm data", which corresponds to include
406 only data collected from Experiment 5 with the three species. Dataset D was
407 used to evaluate the information provided by data collected at concentrations
408 lower than E_{r_a} and E_{r_d} (EC_{50} values) for algae and duckweeds, respectively.
409 Thus, dataset D included all data except those related to duckweeds and algae
410 exposed to the lowest cadmium concentrations ("monospecific data" and "two
411 species data") collected from Experiment 5. All in all, we tested the minimum
412 necessary dataset in terms of species combinations (one, two, or three species)
413 from datasets A, B and C, and of concentration range via dataset D.

414 **6 Results**

415 **6.1 Model fit and parameter estimates**

416 Our MCMC algorithm always consistently converged according to Gelman and
417 Rubin diagnostics for each simulation. The corresponding 2.5%, 50% and 97.5%
418 quantiles of the posteriors for parameters of interest are summarised in Table
419 1. To keep results clear enough, [we only display](#) fitting results from data of
420 Experiment 5 (measured cadmium concentrations of 0, 2.25, 4.50, 6.88 and 9.09
421 $\mu\text{g/L}$) as medians of the credibility band for predicted data on algae dynamics
422 (Figure 2) and daphnid survival (Figure 3). On a general point of view, data
423 were satisfactorily described by the model, with between 91% and 98% of ob-
424 served data encompassed in the 95% credibility band of the predictions for the
425 different species.

426 Marginal posterior distributions of the estimated parameters are shown in SI
427 (Figure S4). We obtained narrow posterior distributions for almost all param-

428 eters, in particular parameters of interest, with the exception of parameters
429 related to algae-daphnids interaction (grazing). The narrowness of posterior
430 distributions indicates that sufficient information was available in the data to
431 get posterior distributions of model parameters that are more precise than their
432 priors. Such a gain of knowledge makes us confident in our fitting process.

433 **6.2 Algae dynamics and daphnid survival**

434 In the presence of duckweeds only (Figure 2(a), control), the number of algal
435 cells per beaker in the water column increased during the first seven days when
436 growth is higher than settling, and then decreased as growth declined while
437 settling was continuing. In the presence of daphnids plus duckweeds, the global
438 algal dynamics in the control was similar to the one without daphnids; however
439 the number of algal cells per beaker was lower, due to daphnid grazing (Figure
440 2(b), control). There was additionally no effect of cadmium on the algal dy-
441 namics when duckweeds were present (Figure 2(a)). However, with daphnids,
442 differences between tested concentrations appeared from the sixth day of exper-
443 iment: the higher the cadmium concentration, the higher the number of algal
444 cells (Figure 2(b)). This may be due to the decrease in daphnid number (Figure
445 3), daphnid survival being highly affected by cadmium, particularly at the two
446 highest tested concentrations C_3 and C_4 .

447 **6.3 Look-back on the experimental design**

448 To take into account the potential effect of correlations between parameters, we
449 compared 95% credibility intervals of the stress functions predicted from the
450 joint posterior distributions obtained for each partial dataset (A to D) to the

451 one obtained from the whole dataset (Figure 4). The 95% credibility intervals
452 of the predicted stress functions on daphnid growth rate and survival for each
453 partial dataset appear superimposed to the 95% credibility intervals of the pre-
454 dicted stress functions for all the data. This result was expected since daphnid's
455 survival and size data were included in all datasets, the whole and partial ones.
456 When "monospecific" data were removed (dataset A), the predicted stress func-
457 tions were different from the reference ones with larger 95% credibility bands,
458 particularly for competition parameter β . When "two species" data were re-
459 moved (dataset B) the predicted stress functions for both algal and duckweed
460 growth rates (r_a and r_d) were very close to the reference ones. On the contrary,
461 the predicted stress function for competition parameter β was overestimated,
462 and showed more uncertainty. When "monospecific" and "two species" data
463 were removed (dataset C), we obtained very large 95% credibility intervals for
464 predicted stress functions for both growth rates and the competition parameter.
465 At last, dataset D (without data related to duckweeds and algae exposed to the
466 lowest concentrations C_1 to C_4) led to very similar predicted stress functions
467 for both algal and duckweed growth rates (r_a and r_d) compared to the refer-
468 ence ones, while for competition parameter β the predicted stress function was
469 overestimated with a greater uncertainty.

470 7 Discussion

471 7.1 Cadmium effect

472 7.1.1 On parameters and processes

473 For parameters related to cadmium effect on algae and duckweeds, we obtained
474 similar estimates to the ones obtained in a previous study involving only these
475 two species [Lamonica et al., 2016b]. However, posterior distributions were nar-
476 rower in the present study for some of the parameters, e.g. E_{r_a} , b_{r_a} , E_β and b_β ,
477 mainly thanks to additional data we considered for fitting.

478 Parameters of the stress function on daphnid survival showed narrow poste-
479 rior distributions. Parameter NEC was estimated at 4.47 [2.95, 5.75] $\mu\text{g/L}$
480 while other authors estimated either higher NEC values (8.6 $\mu\text{g/L}$ [Nebeker
481 et al., 1986]) or lower ones (0.720 [0.0427, 1.78] [Forfait-Dubuc et al., 2012])
482 from monospecific studies. Our NEC estimate was high compared to the one
483 obtained with data from the same microcosm, but including five species and sed-
484 iment, namely 1.8 [1.2, 2.3] $\mu\text{g/L}$ [Billoir et al., 2012]. Nevertheless, the NEC
485 estimated by Billoir et al. was only based on survival data, and thus did not in-
486 clude data related to the dynamics of the other species. In particular, the algae
487 dynamics link to the number of surviving daphnids was ignored. We thus also
488 estimated the NEC only using survival data to compare 95% credible interval
489 to the one of [Billoir et al., 2012]. We obtained a NEC value of 3.47 [0.030, 5.50]
490 $\mu\text{g/L}$. This credible interval is quite large because the number of alive daphnids
491 per beaker was highly variable, but it contains the credible interval obtained by
492 [Billoir et al., 2012]. The number of alive daphnids per beaker revealed difficult
493 to describe because of the high inter-replicate variability between the tested

494 cadmium concentrations.

495 In the literature, the effects of cadmium on daphnid growth may vary a lot
496 from one study to another: $EC_{10} = 7.3 \mu\text{g/L}$ for 17 days in [Knops et al.,
497 2001] (monospecific bioassay conditions), $NEC = 0.15 \mu\text{g/L}$ in [Billoir et al.,
498 2012] (five-species microcosm conditions) or $EC_{50} = 2.7 \mu\text{g/L}$ for 21 days in
499 [Clément et al., 2014] (five-species microcosm conditions). In the present study,
500 such effects are expressed through both parameters b_k and E_k (*i.e.*, EC_{50}).
501 We obtained a very high but imprecise estimate for E_k ($47.9 [18.2, 2042] \mu\text{g/L}$)
502 indicating that daphnids were less sensitive in our experiment than in the one
503 conducted by [Clément et al., 2014]. However, [the low values of curvature coeffi-](#)
504 [cient \$b_k\$](#) ($0.56 [0.21, 1.04] \mu\text{g/L}$) indicated that daphnid growth rate was already
505 affected at the lowest concentrations, as also mentioned by [Billoir et al., 2012].

506 7.1.2 On the functioning of the microcosm

507 The microcosm functioning with cadmium or not is summarised in Figure 5.
508 Cadmium effects on daphnid processes corresponded to a negative direct effect
509 on survival, in particular at concentrations C_3 and C_4 , as well as to a [lighter](#)
510 [negative direct effect on growth \(Figure 4\)](#). These direct effects of cadmium
511 on daphnid processes impact both algae and duckweeds. Indeed they induced
512 a decrease in daphnid grazing that led to an increase in algal density with in-
513 creasing cadmium concentrations. Such a result was supported by the absence
514 of a cadmium effect on algal growth at concentrations below $10 \mu\text{g/L}$, that was
515 a positive indirect effect of cadmium on algae below $10 \mu\text{g/L}$. In addition, there
516 was a negative direct effect of cadmium on the competition intensity. This
517 latter did not compensate the negative direct effect of cadmium on growth of

518 duckweeds, especially since algal density became higher, leading to a decrease
519 in duckweed density.

520 Deciphering the cascade of cadmium effects on the three species is finally possi-
521 ble thanks to our modelling approach coupled with experiments. Unravelling the
522 chemical direct and indirect effects as well as the interactions between species is
523 necessary to correctly interpret the global effect of a chemical substance on the
524 functioning of a species community. Nevertheless, it is much more challenging
525 when the number of species is increasing [Lamonica et al., 2016b]. Hence, the
526 model fits of the present study were overall satisfactory although some predicted
527 data were overestimated compared to observed ones. In particular, the num-
528 ber of algal cells per beaker in the presence of both duckweeds and daphnids
529 were overestimated by our model, as well as the number of duckweed fronds per
530 beaker with algae and daphnids (SI, Figure S2 (b)).

531 **7.2 Look-back on the experimental design**

532 In ecotoxicology, optimising the experimental designs is not a recent concern
533 [Albert et al., 1, Andersen et al., 2000, Forfait-Dubuc et al., 2012, Wright and
534 Bailer, 2006], but today mainly relates to the increasing use of concentration-
535 response or effect models [Chèvre and Brazzale, 2008, Forfait-Dubuc et al., 2012,
536 Holland-Letz and Kopp-Schneider, 2015, Keddig et al., 2015, Khinkis et al.,
537 2003, Sitter and Torsney, 1995, Wang et al., 2006]. As formal optimisation first
538 applied to monospecific bioassays, it mainly focused on the tested concentrations
539 (range and number of concentrations) and on the number of tested individuals
540 (per tested concentration and in total) [Forfait-Dubuc et al., 2012]. Formal op-
541 timisation is less suitable for microcosm experiments because microcosms are

542 more complex devices. Moreover, microcosms are not standardised experimen-
543 tal tools since they are usually set up on a case-by-case basis, according to the
544 specific objectives of the study [Cairns Jr and Cherry, 1997, Crossland and La
545 Point, 1992]. Thanks to our modelling approach, we were able to question the
546 relevance of using certain data to estimate the chosen parameters. Hence, using
547 dataset B provided stress functions similar to the reference ones based on all
548 available data, even though there were changes in individual parameters, which
549 needs to be taken into account when aiming at estimating EC_{50} in particular.
550 We also showed that stress function on the interspecific competition parame-
551 ter (β) from partial dataset D differed from the reference one, while the stress
552 functions on the processes related to growth (for both algae and duckweeds)
553 remained unchanged. Such results suggest that two-species data are not fully
554 necessary, while a larger range of tested concentrations would be strongly rec-
555 ommended to estimate parameters related to effects on interactions between
556 species.

557 Datasets A and B were chosen in order to test if monospecific, respectively
558 two-species, microcosms were necessary to estimate parameters, and dataset C
559 was chosen to test if the complete microcosm alone was sufficient to estimate
560 parameters. Similarly, dataset D was chosen to test if reducing the number of
561 tested concentrations would affect the quality of parameter estimates. Omitting
562 the different species combinations, as well as reducing the number of tested con-
563 centrations, would save a lot of time and experimental effort, especially since
564 adding one concentration to the design implies adding the number of replicates
565 times the number of species combination (and not only the number of repli-
566 cates). Also, cutting off some of the species combinations or some of the tested

567 concentrations would permit to increase the number of replicates per treatment.
568 More replicates may help capture the variability of the system, allowing to bet-
569 ter take uncertainties into account. In addition, when using animal species, the
570 overall objective is to reduce the number of organisms involved in experiments.
571 Even if it remains difficult to know *a priori* which types of data would be ab-
572 solutely necessary to best estimate stress function parameters, the pragmatic
573 look-back we performed using modelling may guide further experiments with
574 microcosms, for instance for other contaminants effects, dynamics under mod-
575 ified abiotic conditions, or even other species interactions. In particular, our
576 study suggests that experiments can be specifically selected to gain knowledge
577 on a three-species microcosm. In the end, we could make the following rec-
578 ommendations for further ecotoxicological studies with a microcosm device: a
579 first experiment with the complete microcosm only (*i.e.*, with the three species)
580 and a tested concentration range limited by the sensitivity of the most sensitive
581 species; then a second experiment with monospecific microcosms only and a
582 tested concentration range limited by the sensitivities of the two less sensitive
583 species. If needed, additional experiments without contaminant may involve
584 different combinations of species depending on their connections to each others.
585 More generally, we would suggest that collecting data of monospecific and com-
586 plete microcosms with contaminant might be sufficient to assess the contaminant
587 effects, as long as in-depth knowledge of the functioning without contaminant
588 is available. Nevertheless, there are limits to how transferable those recommen-
589 dations are. When using another microcosm with different species or additional
590 species, interactions between species still need to be properly investigated with-
591 out contaminant first. Some of the species combinations with contaminant may

592 not be discarded according to the direction or type of the interactions between
593 those species. When using different contaminant, especially contaminants with
594 different mode of action, discarding the lowest concentrations might be an issue.
595 For instance, endocrine disrupting contaminants may show a strong non-linear
596 effect, including effects at low concentrations; in that case scenario low concen-
597 trations should obviously be maintained in the experimental design.

598

599 **8 Conclusion and perspectives**

600 We provided EC_{50} values for the different processes affected by cadmium. Thanks
601 to the understanding of the underlying processes that occurred in the micro-
602 cosm functioning, we also managed to identify the cascade of cadmium effects
603 induced by the interactions between species. In addition, we got back from
604 modelling to experiments in order to determine which of the collected data were
605 necessary and sufficient to precisely estimate model parameters, leading us to
606 suggest a more efficient experimental design. Finally, we (1) highlighted the
607 importance of interactions by identifying the effect cascade occurring within a
608 small ecosystem under chemical pressure; and (2) showed that alternative use
609 of experimental data can help conceiving experimental designs for a microcosm
610 study.

611 Our method also permitted to assess which data to include when estimating
612 parameters of interest in a dynamic ecosystem model from a laboratory based
613 microcosm ecotoxicity study. Such an approach could be enhanced to better
614 foresee further experiments with microcosms based a similar model. Beyond

615 this, if parameters are simultaneously estimated a whole dataset, this makes
616 possible to compare these reference estimates with those obtained with par-
617 tial datasets. This gives knowledge on the data dependency in the modelling
618 results. Last but not least, such a retrospective and descriptive sensitivity anal-
619 ysis puts light in the fact that data quality and design are more beneficial for
620 modelling purpose than quantity. Ideally, as the use of models and big data
621 in ecology increases [Van Den Brink et al., 2016], modellers and experimenters
622 could collaboratively and profitably elaborate model-guided experiments.

623 **9 Figures**

624 **9.1 Figure 1**

625 **9.2 Figure 2 (a) and (b)**

626 **9.3 Figure 3**

627 **9.4 Figure 4**

628 **9.5 Figure 5**

Figure 1: Workflow followed in the present study: (1) in black, development of the model of the microcosm functioning under cadmium pressure, data collection, and estimation of model parameters with the whole dataset, then extraction of stress functions, namely "reference stress functions"; (2) in orange, comparison of population dynamics with and without cadmium to analyse the global perturbation of the community, extraction of EC_{50} for the different processes; (3) in green, build of partial datasets by removing some parts of the complete dataset, estimation of parameters using those partial datasets, comparison of the newly estimated stress functions to the reference ones to assess how much information was provided by the removed data.

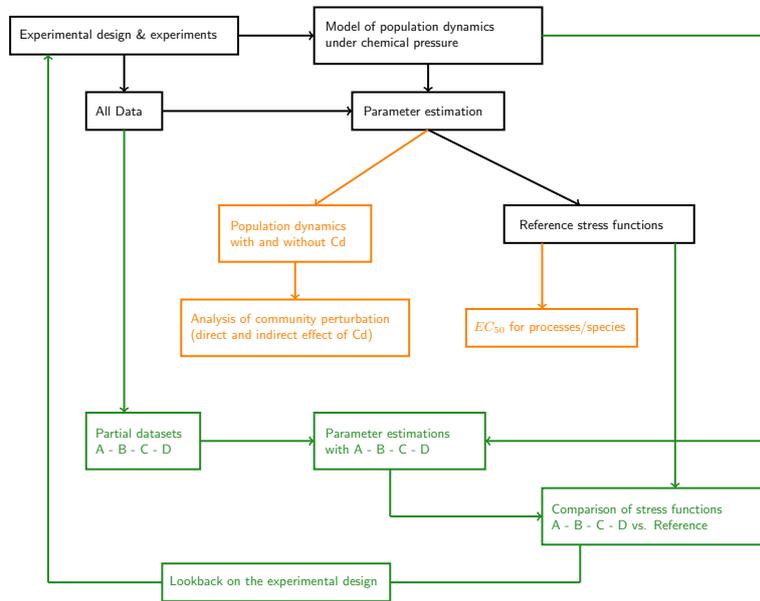


Figure 2: Model fitting for state variables related to algae dynamics: (a) with duckweeds; (b) with duckweeds and daphnids. Symbols refer to the different tested cadmium concentrations of Experiment 5. Plain lines stand for the fitted model with each parameter equal to its median value at each concentration C_j . The light grey area corresponds to the 95% credible band of the predicted data in the control.

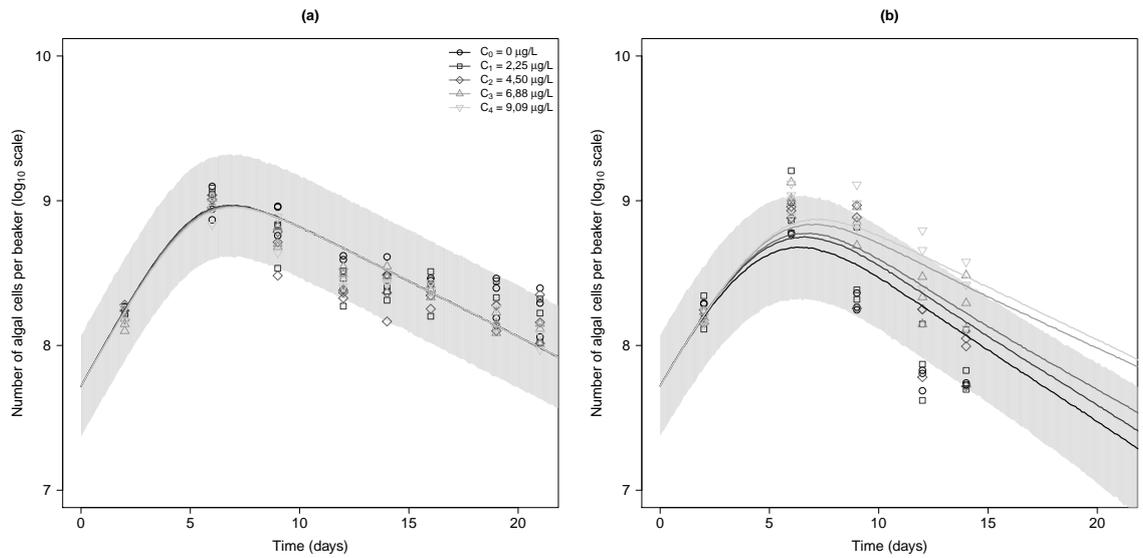


Figure 3: Fit plot for the number of alive daphnids per beaker. Symbols refer to the different tested cadmium concentrations of Experiment 5. Plain lines stand for the fitted model with each parameter equal to its median value at each concentration C_j . The light grey area corresponds to the 95% credible band of the predicted data in the control.

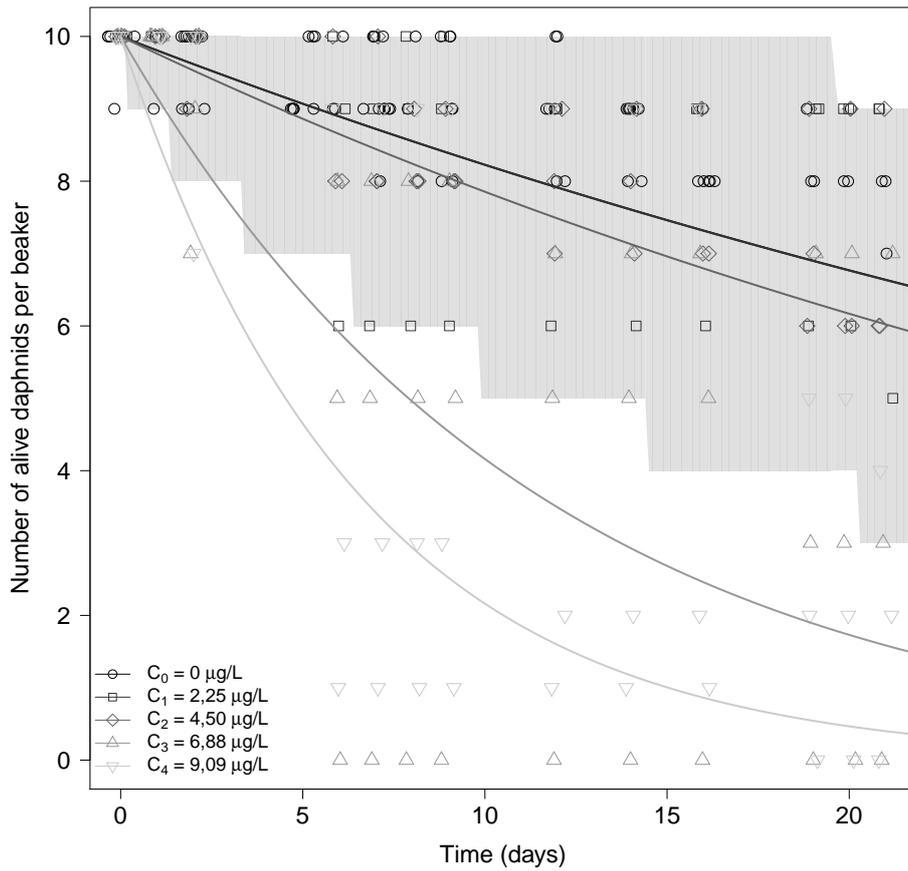


Figure 4: Comparison of stress functions obtained with complete and partial datasets. Plain black lines delimit the 95% credible bands for the stress functions obtained with the partial dataset, while red dotted lines delimit the 95% credible bands for the stress functions obtained with the complete dataset.

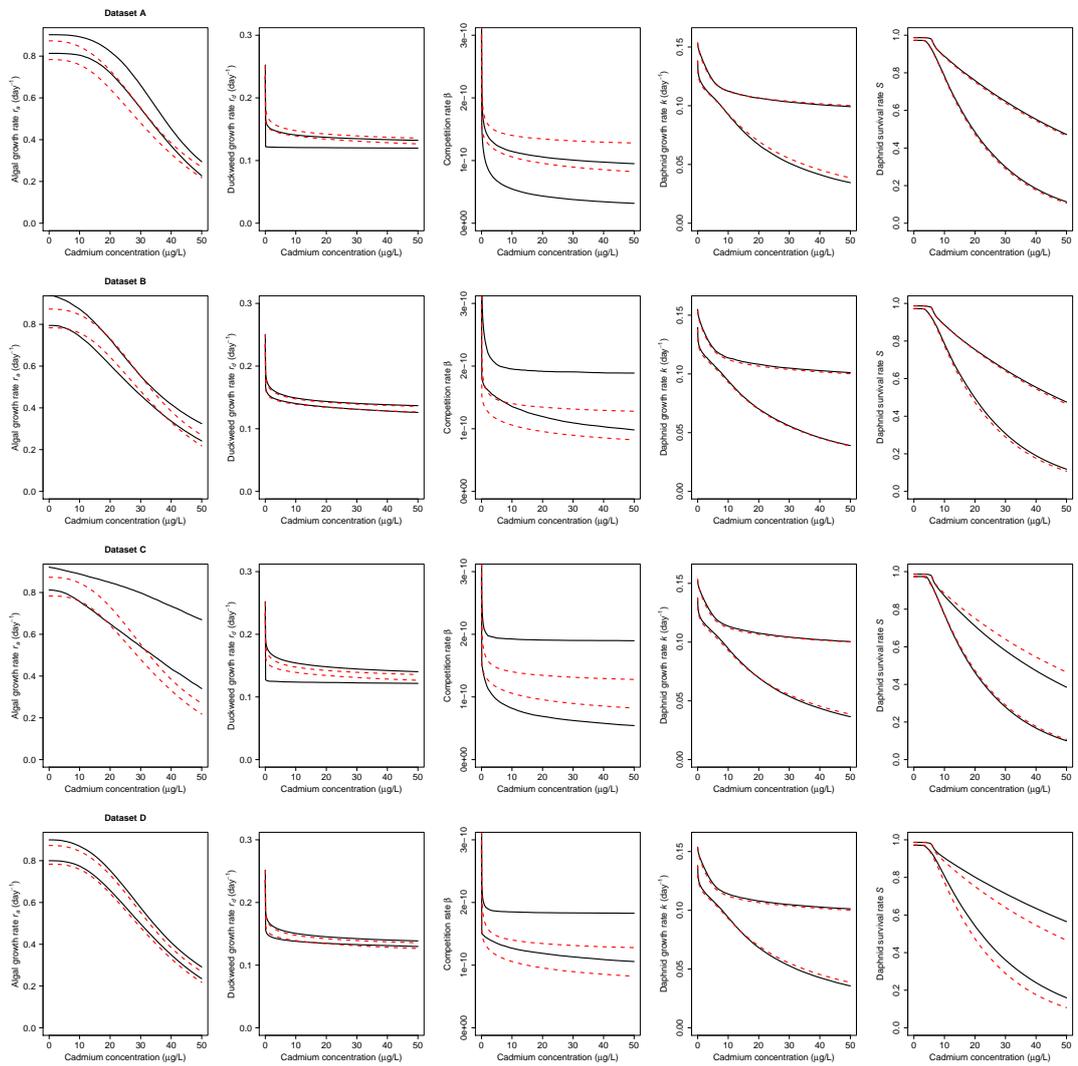
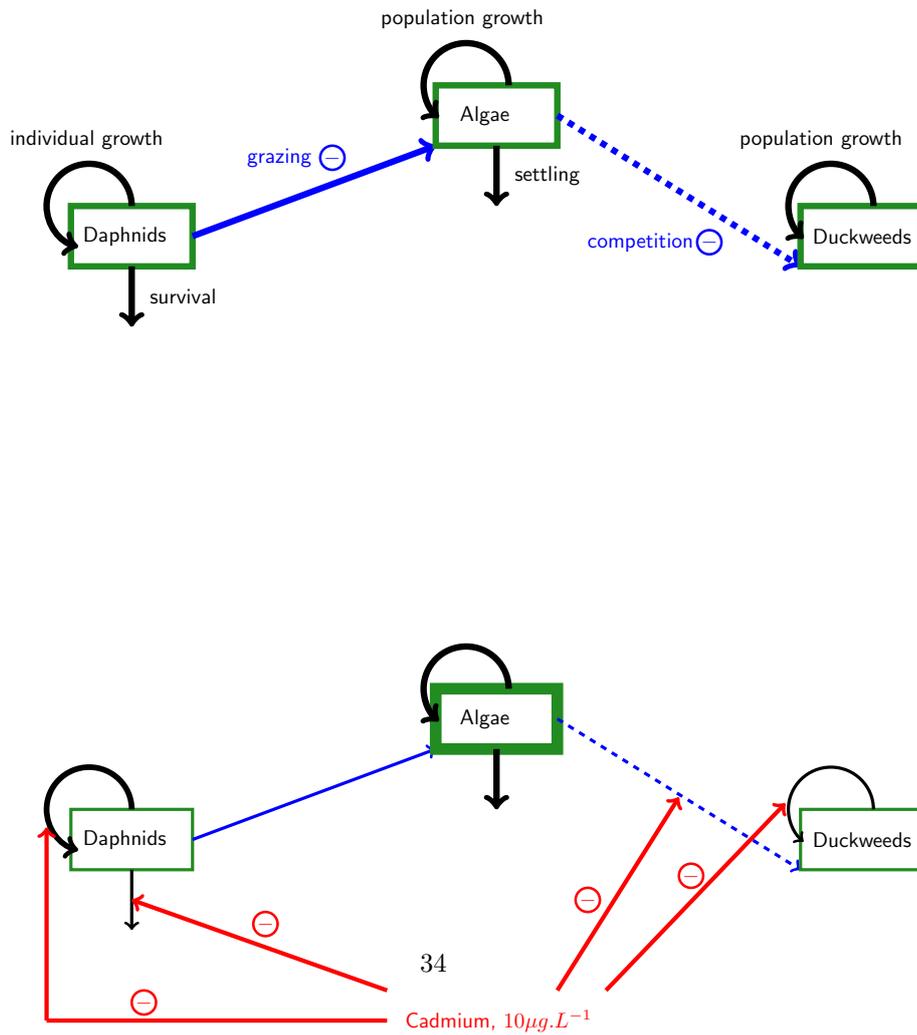


Figure 5: Global perturbation of the microcosm functioning without cadmium (above) and with cadmium ($10 \mu\text{g/L}$, below). Green boxes represent species population, black arrows represent species processes, blue arrows represent interactions between species, red lightnings represent cadmium effect on the different processes. Thickness of boxes lines is proportional to population size and thickness of arrows is proportional to process intensity.



629 **10 Tables**

Table 1: Parameters of interest.

Symbol	Definition	Unit	Prior distribution* or value	Sources**	2.5, 50, 97.5 % posterior quantiles
r_{a_0}	Intrinsic algal growth rate in the control	day ⁻¹	$\mathcal{U}(0,2)$	[1]	0.78 0.83 0.87
E_{r_a}	The concentration at which r_{a_0} is reduced by 50 %	$\mu\text{g.L}^{-1}$	$\log_{10}(E_{r_a}) \sim \mathcal{N}(1.78,0.1)$	[2]	1.54 1.56 1.58
b_{r_a}	Curvature coefficient	-	$\log_{10}(b_{r_a}) \sim \mathcal{N}(0.24,0.1)$	[2]	0.37 0.43 0.49
β_0	Competition intensity of algae on duckweeds in the control	# of cells per beaker ⁻¹ .day ⁻¹	$\log_{10}(\beta_0) \sim \mathcal{U}(-11,-9)$	[2]	-9.53 -9.46 -9.40
E_β	The concentration at which β_0 is reduced by 50 %	$\mu\text{g.L}^{-1}$	$\log_{10}(E_\beta) \sim \mathcal{U}(-1,4)$	Vague	-0.99 -0.77 -0.15
b_β	Curvature coefficient	-	$\log_{10}(b_\beta) \sim \mathcal{U}(-3,3)$	Vague	-1.11 -0.82 -0.62
m_0	Daphnid mortality rate in the control	daphnid.day ⁻¹	$\log_{10}(m_0) \sim \mathcal{U}(-4,0)$	Vague	-1.89 -1.71 -1.56
k_S	Slope of survival stress function	$\mu\text{g}^{-1}.\text{L}.\text{day}^{-1}$	$\log_{10}(k_S) \sim \mathcal{U}(-4,4)$	Vague	-1.80 -1.54 -1.30
NEC	No Effect Concentration on daphnid survival	$\mu\text{g.L}^{-1}$	$\log_{10}(NEC) \sim \mathcal{U}(-2,1)$	Vague	0.47 0.65 0.76
k_0	Daphnid growth rate in the control	day ⁻¹	$\mathcal{N}(0.11,0.030)$	[3]	0.138 0.146 0.154

Symbol	Definition	Unit	Prior distribution* or value	Sources**	2.5, 50, 97.5 % posterior quantiles
E_k	The concentration at which k_0 is reduced by 50 %	$\mu\text{g.L}^{-1}$	$\log_{10}(E_k) \sim \mathcal{U}(-1,4)$		1.26 1.68 3.31
b_k	Curvature coefficient	-	$\log_{10}(b_k) \sim \mathcal{U}(-3,3)$		-0.68 -0.25 0.015
r_{d_0}	Intrinsic duckweed growth rate in the control	day^{-1}	$\mathcal{U}(0,2)$	[2]	0.23 0.24 0.25
E_{r_d}	The concentration at which r_{d_0} is reduced by 50 %	$\mu\text{g.L}^{-1}$	$\log_{10}(E_{r_d}) \sim \mathcal{N}(2.44,0.2)$	[2]	1.96 2.30 2.67
b_{r_d}	Curvature coefficient	-	$\log_{10}(b_{r_d}) \sim \mathcal{U}(-3,3)$	Vague	-1.05 -0.91 -0.77

⁶³⁰ *Prior distribution: \mathcal{N} stands for the normal law, \mathcal{U} stands for the uniform law.

⁶³¹ **Sources: [1] [Lamonica et al., 2016a], [2] [Lamonica et al., 2016b], [3] [Billoir et al.,

⁶³² 2008].

Table 2: Experimental design and partial datasets.

Cadmium concentrations	Monospecific data	Two species data	Complete microcosm data
C_0	Algae	Algae, duckweeds	Algae, duckweeds, daphnids
	Duckweeds	Algae, daphnids	
C_{1-4}	Algae	Algae, duckweeds	Algae, duckweeds, daphnids
	Duckweeds		
C_{5-8}	Algae	Algae, duckweeds	
	Duckweeds		
C_{9-12}	Algae		

633 The black dashed, gray dashed, black and gray rectangles refer to the data that
634 have been removed from the entire dataset to build partial dataset A, B, C and D,
635 respectively.

636 Data accessibility

637 Data are available online: <https://doi.org/10.5281/zenodo.6598408>

638 Supplementary material

639 R scripts are available online: <https://doi.org/10.5281/zenodo.6598408>

640 Acknowledgements

641 Authors thank the ENTPE (École Nationale des Travaux Publics de l'État) and IXXI
642 institute (Institut Rhônalpin des Systèmes Complexes) for their financial support.
643 Authors also thank Pauline Le Quellec et Ludovik Hauduroy for their contribution to
644 the experiments. Finally, authors thank the reviewers for their very useful comments

645 and suggestions.

646 **Conflict of interest disclosure**

647 The authors of this preprint declare no financial conflict of interest with the content
648 of this article.

649 **Appendix**

650 Supplementary Information is available online: <https://doi.org/10.5281/zenodo.6598408>

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